

Exponents 4^2

I have included a voice recorded power point show that has automatic slide advancement. Please leave feedback if you find this helpful, and I will go back and add it to my other units.

Preview

I have also started adding detailed lesson plans to my units. Please leave feedback on if this addition is helpful to you!!

***For Middle/High School
Special Education***



Exponents Lesson Plan

Preparation

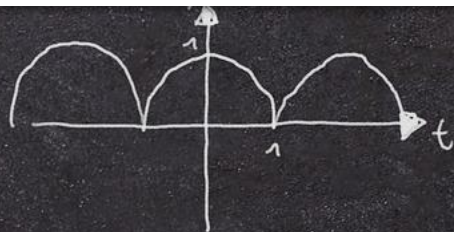
- Print out a vocabulary board for each student to use throughout unit
 - Laminate or place in page protector
- Book
 - Print out, laminate, and bind
 - OR your students can listen to the pre-recorded version
- Vocabulary cards
 - Print out a set of cards onto cardstock and laminate
 - Make one set for each student and one for the teacher to use in 1 Spy games

Preassessment (do day 1 before starting lesson)

- Choose the form of the assessment that best fits the learning level of your students
- Give the assessment to assess what your students may already know
- I cannot emphasize enough how important this step is. If you want to see growth, this preassessment is so important!!

Teaching Tips

- Color Coding:** this is a really easy way to add more structure to a matching activity. Outline or color in an empty box or sorting label. Outline or color in the corresponding picture symbols the same colors. Becomes a color matching task.
 - For more info, read more here: <https://specialneedsforspecialkids.org/2015/09/05/using-color-coding-for-differentiation/>
 - I also have a blog post on differentiating one activity 3 ways: <https://specialneedsforspecialkids.org/2018/10/22/differentiating-1-activity-3-ways-easily-and-effectively/>
- Make your own copies of the activities:** Every day I review the activity we did yesterday. For that reason:
 - I often complete the activity myself and often laminated it for easy rev that I could use year after year.
 - My copies were also helpful as either a model for students who needed more support or as a way for more advanced students to self-check the work.



$$2L=2 \Rightarrow L=1$$

$$a_n \approx \frac{1}{n^2}$$

$$b_n = \emptyset$$

Lesson Plans

13 days

$$\left[\frac{n\pi t}{L} \right] + b_n \cdot \sin \left(\frac{n\pi t}{L} \right)$$

Quick Look

Day	Activity	Day	Activity
1	<ul style="list-style-type: none"> Book: Exponents Vocabulary activity Repeated addition and multiplication with models worksheets 	7	<ul style="list-style-type: none"> Book: Sequences Vocabulary activity Arithmetic or geometric sequences worksheets
2	<ul style="list-style-type: none"> Book: Exponents Vocabulary activity Repeated addition and multiplication with models worksheets 	8	<ul style="list-style-type: none"> Book: Sequences Vocabulary activity Arithmetic or geometric sequences worksheets
3	<ul style="list-style-type: none"> Book: Exponents Vocabulary activity Match equivalent expressions with exponents worksheets 	9	<ul style="list-style-type: none"> Book: Graphing Vocabulary activity Linear or exponential graph
4	<ul style="list-style-type: none"> Book: Exponents Vocabulary activity Match equivalent expressions with exponents worksheets 	10	<ul style="list-style-type: none"> Book: Graphing Vocabulary activity Linear or exponential graph
5	<ul style="list-style-type: none"> Book: Sequences Vocabulary activity Arithmetic or geometric sequences worksheets 	11	<ul style="list-style-type: none"> Book: your choice Vocabulary cut and paste Sudoku puzzle
6	<ul style="list-style-type: none"> Book: Sequences Vocabulary activity Arithmetic or geometric sequences worksheets 	12	<ul style="list-style-type: none"> Book: your choice Vocabulary cut and paste Close worksheets
		13	<ul style="list-style-type: none"> Review if needed (plenty of extra worksheets) Assessment

Day 7

Activity	Notes	Materials
Read or listen to a recording of the book: Sequences (10 minutes)	<ul style="list-style-type: none"> Read through the story, asking lots of questions Continue to make connections between book and vocabulary board 	<ul style="list-style-type: none"> Book Vocabulary board
Vocabulary cards Go Fish Game (minutes)	<ul style="list-style-type: none"> Using several completed student sets of vocabulary cards play a traditional go fish game <ul style="list-style-type: none"> Modify/use devices or buddies as needed for additional support 	<ul style="list-style-type: none"> Vocabulary cards (student sets) Vocabulary board
Worksheet (minutes)	<ul style="list-style-type: none"> Review the worksheet completed yesterday 	<ul style="list-style-type: none"> System of equations worksheet
Arithmetic and geometric sequences worksheets (minutes)	<ul style="list-style-type: none"> This next set of worksheets has a differentiated version included. Choose the best level for your students Do 1-2 of the worksheets 	<ul style="list-style-type: none"> Worksheet
Graphing (minutes)	<ul style="list-style-type: none"> Each student shares one of their finished worksheets with the group using the communication method of their choice 	<ul style="list-style-type: none"> Completed worksheets Communication devices

$$\frac{1}{2} \int_0^1 f(t) dt$$

$$\int_0^1 1 dt$$

$$[t]_0^1$$

$$a_n \rightarrow a(\omega)$$

$$b_n \rightarrow b(\omega)$$

$$\sqrt{a(\omega)^2 + b(\omega)^2}$$

When you see a number that has an exponent, it is a combination of two numbers. The larger number is called the **base**. In this example, the base is 2.

$$2^4$$

3 short books

The exponent tells you how many times to multiply the base to itself. Like this:

$$2^4 = 2 \times 2 \times 2 \times 2$$

Arithmetic sequences are helpful, because once we determine the pattern, or common difference, we can predict future values.

$$5, 10, 15, 20, 25, ?, ?$$

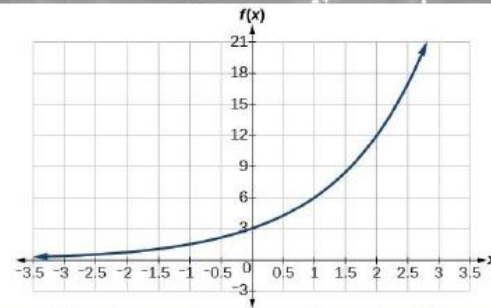
+5 +5 +5 +5 +5 +5

This is an example of a different type of sequence. It is a **geometric sequence**. A geometric sequence increases by a constant called a **common ratio**.

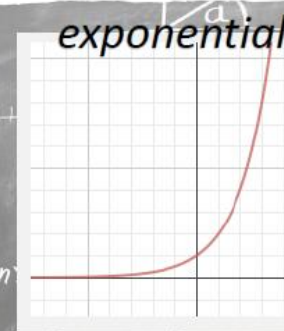
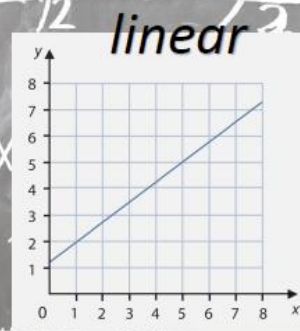
$$2, 4, 8, 16, 32, 64$$















x2 x2 x2 x2 x2

You probably noticed that numbers get really big quickly when you use exponents. That means the graphs are going to look different too.



Let's look at them side by side:






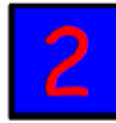
 base	 exponent	 power	 repeated	 addition
 multiplication	 squared	 cubed	2, 4, 6, 8, 10 sequence	+? common difference
x? common ratio	x,y variable	 linear	 exponential	 graph
 please repeat	 yes	 no	I don't know	I need a break

Vocabulary board

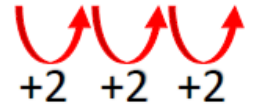


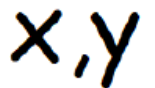
14 vocab cards

<p>cubed</p> <p>When the exponent is 3.</p> <div style="border: 1px solid black; width: 60px; height: 60px; margin: 10px auto;"></div>	<p>sequence</p> <p>A progression of numbers.</p> <div style="border: 1px solid black; width: 60px; height: 60px; margin: 10px auto;"></div>
<p>arithmetic sequence</p> <p>When a sequence of numbers increases or decreases by a constant value.</p> <div style="border: 1px solid black; width: 60px; height: 60px; margin: 10px auto;"></div>	<p>geometric sequence</p> <p>When a sequence of numbers increases by a fixed multiple.</p> <div style="border: 1px solid black; width: 60px; height: 60px; margin: 10px auto;"></div>

Cut & Paste

<p>exponent</p> <p>Smaller number slightly above the base that tells what the power the base is raised to.</p> <div style="text-align: center;"></div>	<p>base</p> <p>The main number in the expression involving an exponent <i>that is multiplied</i> a repeated number of times.</p> <div style="text-align: center;"></div>
<p>power</p> <p>The smaller number in the expression involving an exponent that tells you <i>how many times</i> to multiply.</p> <div style="text-align: center;"></div>	<p>squared</p> <p>When the exponent is 2.</p> <div style="text-align: center;"></div>

$$= \frac{1}{2c} \int f(t) dt$$

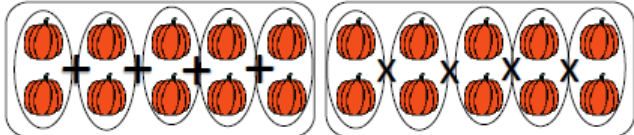
<p>The main number in the expression involving an exponent <i>that is multiplied</i> a repeated number of times.</p>	<p>common difference</p> <div style="border: 1px solid black; width: 100px; height: 40px; margin: 5px auto;"></div>	<p>common ratio</p> <div style="border: 1px solid black; width: 100px; height: 40px; margin: 5px auto;"></div>
<p>Terms that are unknown or changing in an equation, often represented by letters.</p>	<div style="text-align: center;"></div>	<div style="text-align: center;"></div>
<p>When a sequence of numbers increases by a fixed multiple.</p>	<p>equation</p> <div style="border: 1px solid black; width: 100px; height: 40px; margin: 5px auto;"></div>	<p>variables</p> <div style="border: 1px solid black; width: 100px; height: 40px; margin: 5px auto;"></div>
<p>Fixed multiple that each number is multiplied by in a geometric sequence.</p>	<div style="text-align: center;"></div>	<div style="text-align: center;"></div>

Either draw or use the picture on the next page to draw each equation. The first one is done as an example.

Optional: have students use a calculator to figure total and circle the one with the most.

2×5

2^5



$2 + 2 + 2 + 2 + 2$

$2 \times 2 \times 2 \times 2 \times 2$

3×3

3^3

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Match equivalent expressions

Circle or shade in the equivalent expression

1. 7^2

$2+2+2+2+2+2$

7×7

$7 + 7$

2. 4^3

$4 \times 4 \times 4$

4×3

$3 + 3 + 3 + 3$

3. 6^4

6×4

$6 + 6 + 6 + 6$

$6 \times 6 \times 6 \times 6$

4. 2^2

$2 + 2$

2×2

$2 \times 2 \times 2 \times 2$

5. 1^8

$1 \times 1 \times 1 \times 1 \times 1 \times 1 \times 1 \times 1$

$1 + 1 + 1 + 1 + 1 + 1 + 1 + 1$

1×8

Draw a line to the equivalent expression.

10^2

$3 \times 3 \times 3 \times 3 \times 3 \times 3$

7^3

$7 \times 7 \times 7$

4^4

10

Find the equivalent expression.

10^2

9^5

4×4

2^4

8^6

$9 \times 9 \times$

6^6

3^7

$8 \times 8 \times 8$

8^3

12^3

$8 \times 8 \times 8$

$12 \times 12 \times 12$

$2 \times 2 \times 2 \times 2$

10×10

1×1

$6 \times 6 \times 6 \times 6 \times 6 \times 6$

Repeated addition and multiplication with models

Different formats

$u=2 \Rightarrow L=1$

$a_n \approx \frac{1}{n^2}$

$b_n = \emptyset$

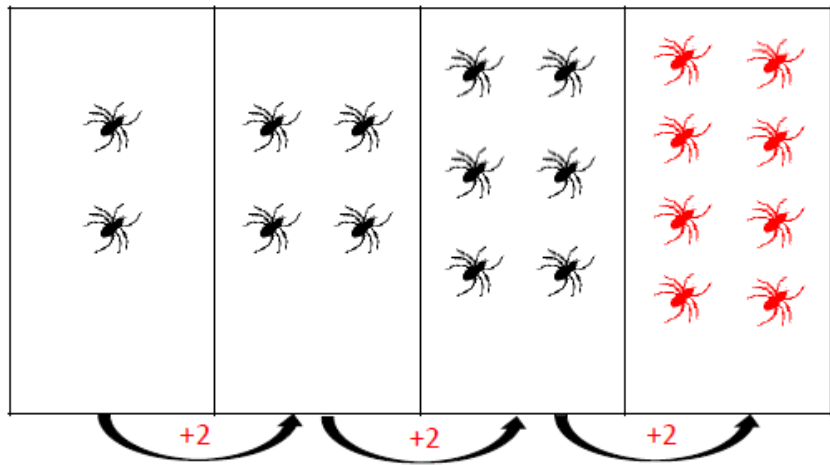
$\rightarrow a(w)$

$\rightarrow b(w)$

Draw or use the pictures to complete each arithmetic sequence.

Sample

Common difference



Finding the common difference in the arithmetic sequence. The first one is done as an example.

2, 4, 6, 8, 10
 $\xrightarrow{+2}$ $\xrightarrow{+2}$ $\xrightarrow{+2}$ $\xrightarrow{+2}$

Common difference

3, 4, 5, 6, 7

Common difference

10, 20, 30, 40, 50

Common difference

3, 6, 9, 12, 15

Common difference

0, 5, 10, 15, 20

Common difference

Finding the common difference in the arithmetic sequence. The first one is done as an example.

2, 4, 6, 8, 10
 $\xrightarrow{+2}$ $\xrightarrow{+2}$ $\xrightarrow{+2}$ $\xrightarrow{+2}$

Common difference

3, 4, 5, 6, 7
 $\xrightarrow{+1}$ $\xrightarrow{+1}$ $\xrightarrow{+1}$ $\xrightarrow{+1}$

Common difference

10, 20, 30, 40, 50
 $\xrightarrow{+10}$ $\xrightarrow{+10}$ $\xrightarrow{+10}$ $\xrightarrow{+10}$

Common difference

3, 6, 9, 12, 15
 $\xrightarrow{+3}$ $\xrightarrow{+3}$ $\xrightarrow{+3}$ $\xrightarrow{+3}$

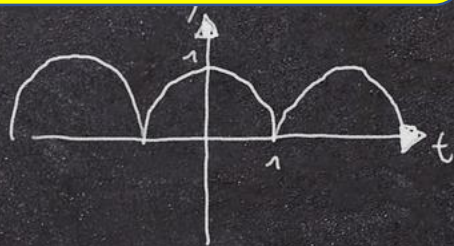
Common difference

0, 5, 10, 15, 20
 $\xrightarrow{+5}$ $\xrightarrow{+5}$ $\xrightarrow{+5}$ $\xrightarrow{+5}$

Common difference

Arithmetic & Geometric sequences

Sequences with pictures



$2L=2 \Rightarrow L=1$

$a_n \approx \frac{1}{n^2}$

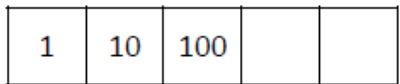
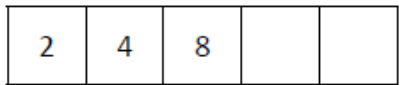
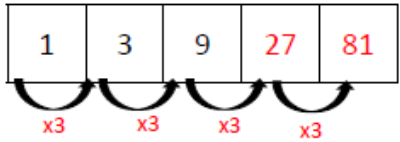
$b_n = \emptyset$

Differentiated

$= \frac{1}{2} \int f(t) dt + \frac{1}{2} \int_0^1 1 dt + \frac{1}{2} \int_0^1 1 dt$
 $= \frac{1}{2} [-t]_{-1}^0 + \frac{1}{2} [t]_{-1}^1$

$\sqrt{a(\omega)^2 + b(\omega)^2}$

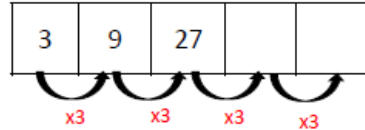
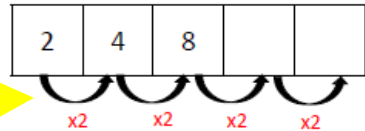
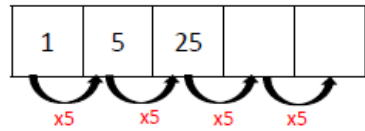
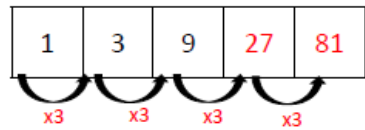
Look at the following **geometric sequence** and predict what comes next. The first one is done for you. Students may need a calculator.



Arithmetic & Geometric sequences

$$a_n \cdot \cos\left(\frac{n\pi L}{L}\right) + b_n \cdot \sin\left(\frac{n\pi L}{L}\right)$$

Look at the following **geometric sequence** and predict what comes next. The first one is done for you. Students may need a calculator.



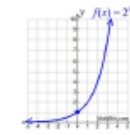
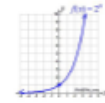
Differentiated

$u=2 \Rightarrow L=1$
 $a_n = \dots$
 $b_n = \emptyset$

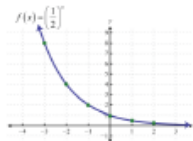
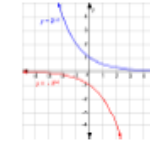
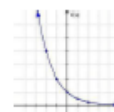
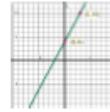
Circle or shade in all the graphs showing a **linear** function or equation.

Circle the correct graph.

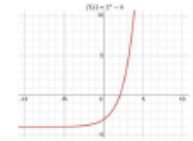
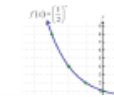
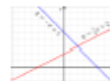
1. linear



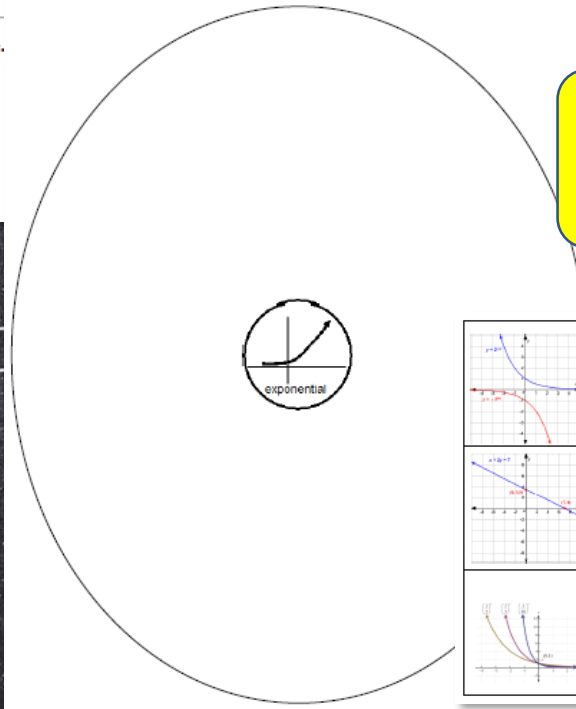
2. exponential



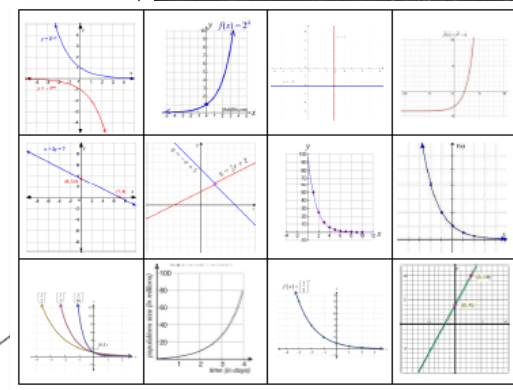
3. linear



4.



Id graphs: 3 formats



(3)
(3)

Exponents

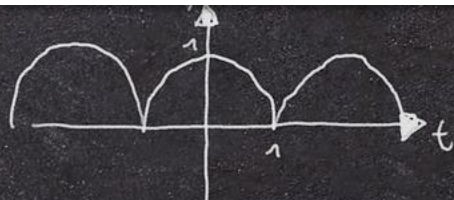
1. Exponents are an example of multiplication.

2. Exponents are written in a special way. The is the large number.

3. The number is the exponent.

4. The exponent tells you how many time the base is .

5. The exponent of is also called squared.



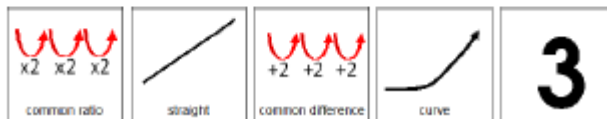
Close worksheets

$$b_n = \emptyset$$

Exponents (page 1)



Exponents (page 2)



Exponents

6. A cubed exponent is represented by the number .

7. Geometric sequences increase by a .

8. Arithmetic sequences increase by a .

9. A linear graph will have a line.

10. An exponential graph has a line that due to such a rapid rate of change.

Exponents

			2^4 exponent	$=$ equation
			$+2$ common difference	$\times 2$ common ratio
	$\times 2$ common ratio		2 squared	$=$ equation
			$+2$ common difference	
$=$ equation		2 squared		2^4 exponent

			2 squared	2 squared
2 squared	2 squared	$+2$ common difference	$+2$ common difference	$+2$ common difference
$+2$ common difference	$\times 2$ common ratio	$\times 2$ common ratio	$\times 2$ common ratio	$=$ equation
$=$ equation	$=$ equation	2^4 exponent	2^4 exponent	2^4 exponent

Sudoku
4x4 also included

$$\int f(t) dt$$

$$\int f(t) dt + \frac{1}{2} \int f(t) dt$$

$$t dt + \frac{1}{2} \int_0^1 t dt$$

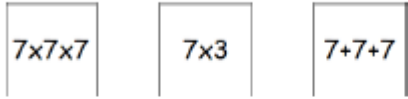
$$t^0 + \frac{1}{2} [t]$$

$$b(w)$$

1. Circle the model that shows 3^2



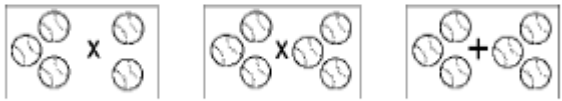
2. Circle the expression that is the same as 7^3



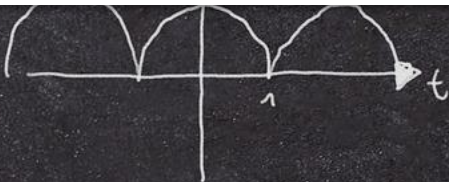
3. Which of the following shows the exponent base circled?



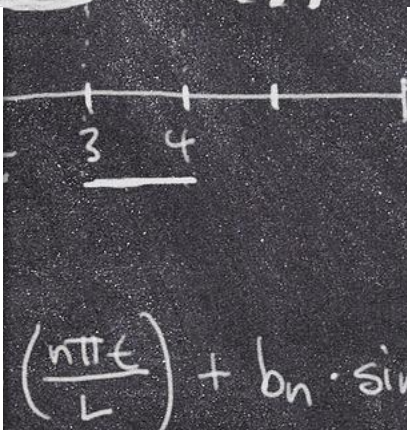
4. Which model shows a number that is squared?



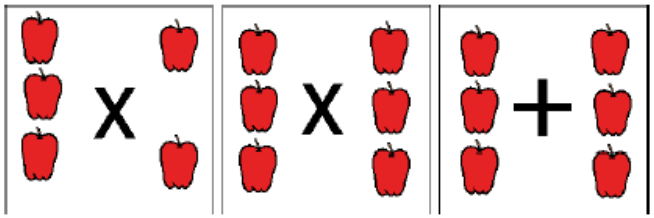
5. How do you write four raised to the fifth power?



$2c=2 \Rightarrow c=1$
 $a_n \approx \frac{1}{n^2}$
 $b_n = \emptyset$



Q1



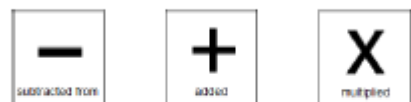
Q2



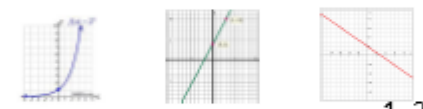
6. A common difference is how much is _____ from one number to the next in a sequence.



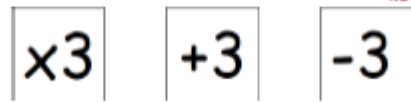
7. A common ratio is how much is _____ from one number to the next in a sequence.



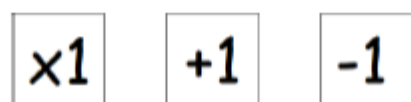
8. Circle the graph that shows an exponential function.



9. What is the common ratio in this sequence: 1, 3, 9, 27



10. What is the common difference in this sequence: 3, 4, 5, 6, 7



$\sqrt{a(\omega)^2 + b(\omega)^2}$
 ω

7. A common ratio is how much is _____ to one number and to the next in a sequence.

- A. subtracted from
- B. added
- C. multiplied

8. Circle the graph that shows an exponential function.



9. What is the common ratio in this sequence: 1, 3, 9, 27

- A. x3
- B. +3
- C. -3

10. What is the common difference in this sequence: 3, 4, 5, 6, 7

- A. x1
- B. +1
- C. -1

Assessments :
 3 versions

$\frac{1}{2} \int_0^1 f(t) dt$
 $\frac{1}{2} \int_0^1 1 dt$
 $\frac{1}{2} [t]_0^1$